

Economics of Risk and Uncertainty

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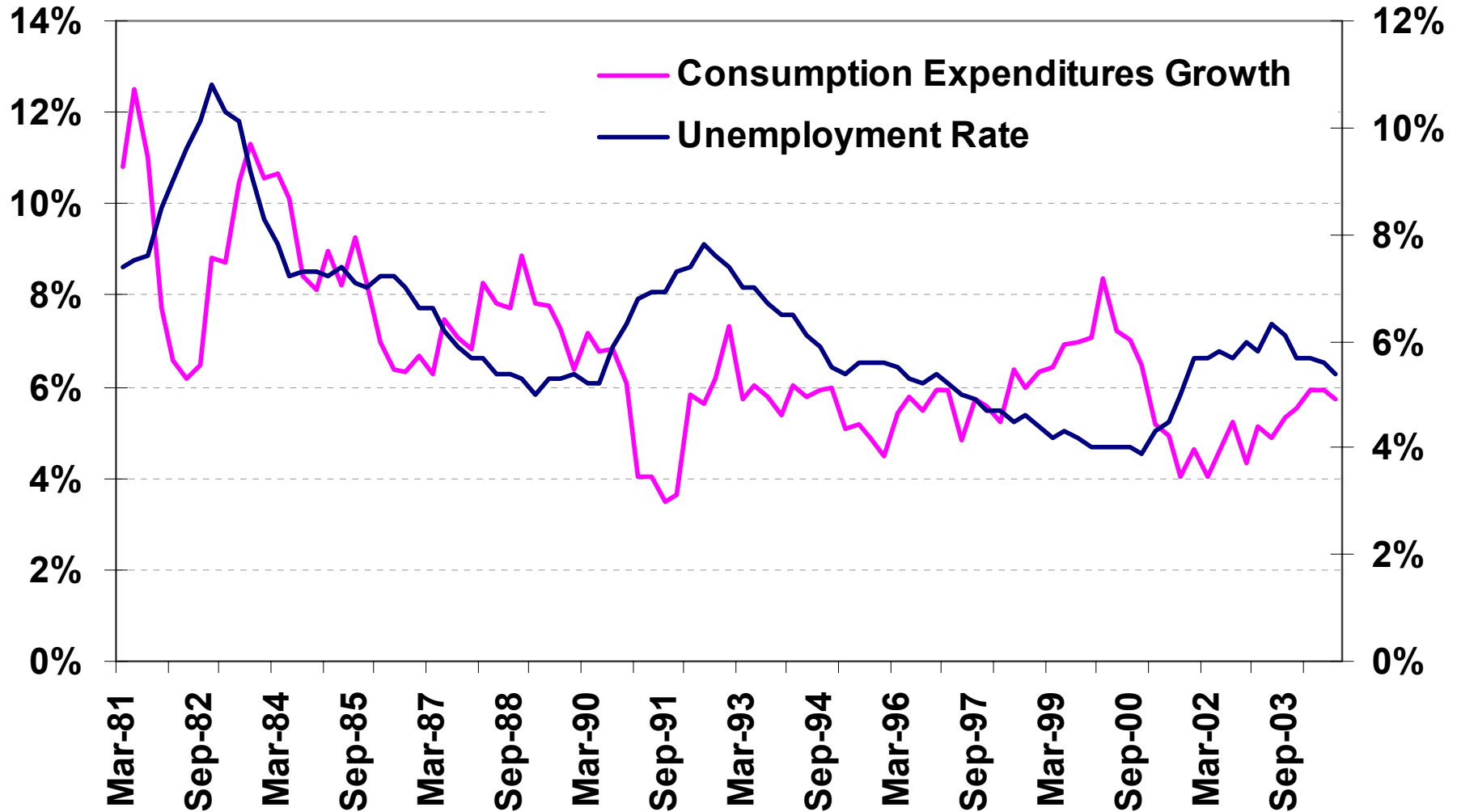
Chapters 4, 5 and 6

4. Consumption and Risk

Outline

- A simple two-period model
- The notion of prudence
- How large are precautionary savings?
- Savings and portfolio choices
- Recursive preferences

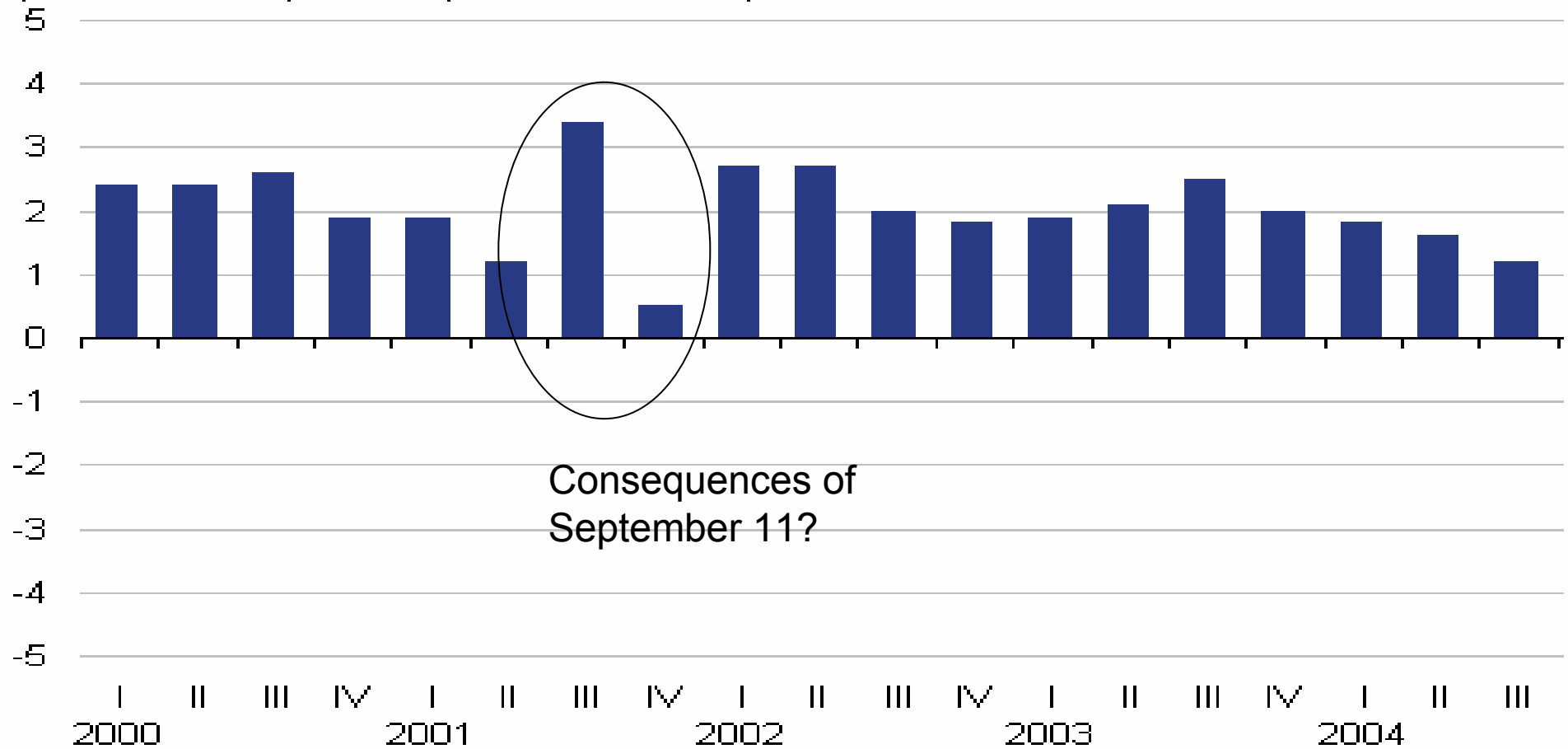
Consumption vs. Unemployment Rate



Source: Bureau of Economic Analysis, 2004

Personal Saving Rate

(Percent of disposable personal income)



Consequences of
September 11?

Objective

- How does risk affect consumption? What is the part of savings that can be attributed to risk?
- Use the simplest microeconomic framework to examine the effect of risk on consumption and savings
- Will explore basic variant versions of this model

Two-Period Model

$U(c_1, c_2) = u(c_1) + \beta v(c_2)$ where β is a discount factor

Assume u, v strictly increasing and concave and thrice differentiable

y_1, y_2 : income in period 1 and 2

Budget constraint:

$$\rho y_1 + y_2 = \rho c_1 + c_2$$

where ρ is the interest factor (one plus the interest rate)

The Model

Let $w = \rho y_1 + y_2$ the future value of total income

The problem is:

1- $\text{Max}_c u(c) + \beta v(w - \rho c)$

Under a (pure) risk on future income ($y_2 + X$) the problem becomes :

2- $\text{Max}_c u(c) + \beta E v(w + X - \rho c)$ where $EX = 0$

Objective: Compare the two maximization problems

FOC, SOC

Certainty:

$$\text{FOC: } u'(c^*) - \beta \rho v'(w - \rho c^*) = 0$$

$$\text{SOC: } u''(c) + \beta \rho^2 v''(w - \rho c) < 0$$

Uncertainty:

$$\text{FOC: } u'(c^{**}) - \beta \rho E v'(w + X - \rho c^{**}) = 0$$

$$\text{SOC: } u''(c) + \beta \rho^2 E v''(w + X - \rho c) < 0$$

Precautionary savings = $c^* - c^{**}$ = reduction in current consumption due to a future income risk

(Assume interiority)

Precautionary Savings

Are precautionary savings positive?

Intuitively: Yes, under risk-aversion. Wrong!

Formally: True if for all β , ρ , w and X

$$u'(c^*) - \beta \rho E v'(w + X - \rho c^*) \leq 0 = u'(c^*) - \beta \rho v'(w - \rho c^*)$$

Equivalent to: for all z and X , $E v'(z + X) \geq v'(z + EX)$

Precautionary Savings

For all X , $E v'(z+X) \geq v'(z+EX)$

By Jensen $\Leftrightarrow v'$ convex, or $v''' \geq 0$

Not risk-aversion, but aversion to downside risk

This condition, $v''' \geq 0$, is commonly known as the condition of « prudence » (Kimball, 1990, Etca)

Early literature: Leland (1968, QJE)

Intuition

What matters is **not** how risk « hurts » utility (risk-aversion) ... but how risk « hurts » marginal utility of income (« prudence »)

Prudence: one unit of wealth has more value under uncertainty

⇔ Aversion to a downside risk : uncertainty has more negative impact when less wealthy

Remark: Multiperiod**

Let the indirect utility function:

$$U(w) = \text{Max}_c u(c) + \beta u(w - \rho c).$$

If u risk-averse (resp. prudent) then U is risk-averse (resp. prudent) as well.

This suggests that the results can usually be extended to multiperiod.

See Carroll and Kimball (1996, Etca)

Remark: Increase in Risk**

Can be extended to any increase in risk in the sense of Rothschild and Stiglitz (1970).

Depends on whether $f(x) = u'(c) - \beta p v'(w+x - pc)$ is concave in x for all the values of the parameters

=> prudence

How Large are Precautionary Savings?

- Controversies
- Dynan (1993, JPE) find little evidence for precautionary savings. Relative prudence - i.e., formally $-xv'''(x)/v''(x)$ - is estimated to be equal to #0.3 => very small and inconsistent with CRRA utility function
- In contrast, Guiso et al. (JME) and Carroll and Samwick (1998, REStat) find significant precautionary savings motive

Exercise

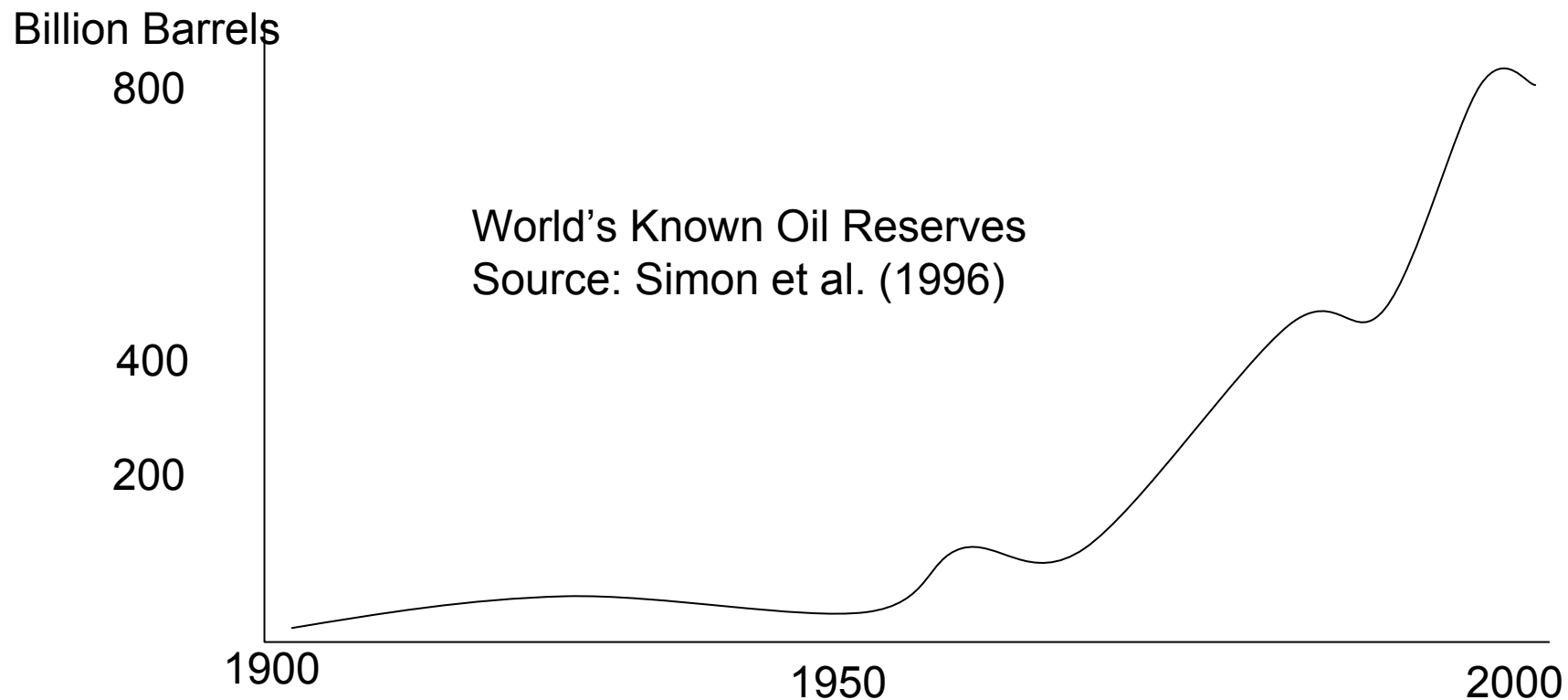
Exercise 1 Let $\text{Max}_c u(c) + \beta E_R v(R(y_1 - c))$ where R is random (capital) risk.

- i) Examine the effect of more capital risk on consumption

- ii) Compare the NS condition to that of prudence. Discuss.

Remark: Exhaustible Resource

Controversies about the size of resources.
Meadows (1972)'s « Limits to Growth »: out of oil in 1992!



Exhaustible Resource Exploitation

- Problem of the optimal exploitation under resource uncertainty
- « How to eat a cake of an unknown size? »
- Similar problem to that analyzed in this chapter (Formally, assume $w+X$ is the size of the resource, and $\rho=1$)

Consumption and Portfolio

Can save in two assets: a risky asset, and a riskless asset

The amount a is invested in the risky asset with a random return of $1+R$; the rest, that is $y_1 - c_1 - a$, is invested in the riskfree asset with a return $1+r$

$$u(c) + \beta E_R u(y_2 + (y_1 - c - a)(1+r) + a(1+R))$$

Basically equivalent to

$$u(c) + \beta E_Z u(w - c + aZ)$$

Consumption and Portfolio (cont'd)

$$\text{Max}_{c,a} u(c) + \beta E u(w - c + aZ)$$

FOCs:

$$EZu'(w - c^* + a^*Z) = 0$$

$$u'(c^*) - \beta E u'(w - c^* + a^*Z) = 0$$

SOCs satisfied

Assume interiority

Drèze and Modigliani (1972, JET)

Consumption and Portfolio (cont'd)

Exercise 2: Assume u CRRA

Show:

$a^* = k^*(w-c)$ proportional to current wealth $(w-c)$

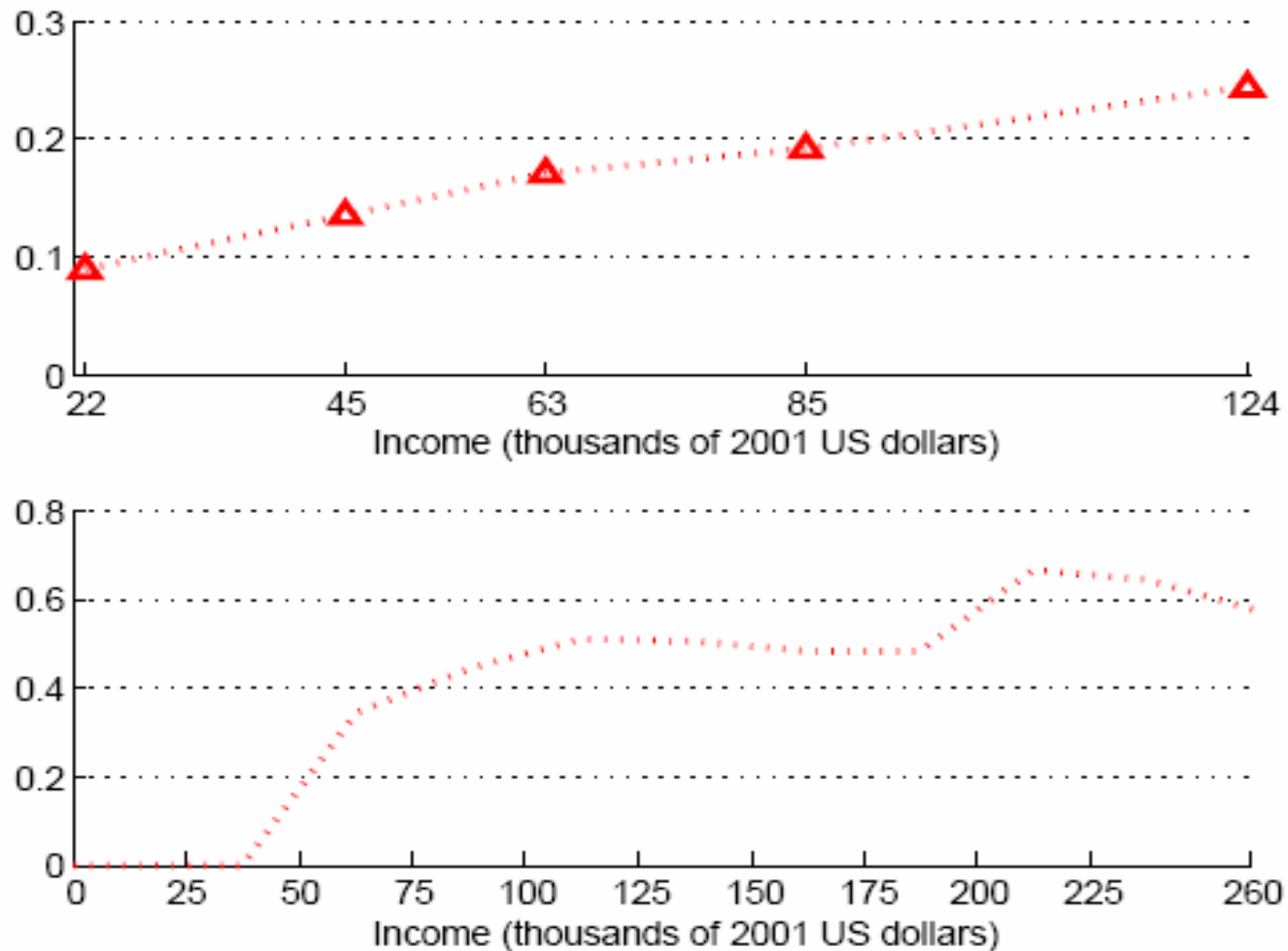
$c^* = m^*w$ proportional to wealth w

with :

k^* defined by $EZ(1+k^*Z)^{-\gamma} = 0$ and

m^* defined by $(m^*)^{-\gamma} - \beta E((1-m^*)(1+k^*Z)^{-\gamma}) = 0$

Figure 1: Empirical Income Expansion Paths for Saving Rates (Upper Diagram) and Equity Shares (Lower Diagram)



Source: Binswanger (2005) based on data on 17,670 consumers from PSID, and SCF

Horizon Length and Consumption

- Within a consumption model, we can consider different horizon lengths. So we can examine the effect of age.
- Young have a longer horizon, i.e. more periods to live. => Can compare the risk preferences of « young » people to those of « old » people
- Should the young be less risk averse?

A Simple Model**

An individual has only one period to live (the old).
His income in the current period is y , and utility $u(y)$

The young has two periods to live. Income y in each period. He can smooth consumption

$$\Rightarrow v(y) = \text{Max}_c u(c) + \beta u(y + \rho(y - c))$$

Exercise 3:

- i) Show that if $\beta\rho=1$, the young and the old have the same risk-aversion towards risk on income y
- ii) Show that under CRRA utility, they have the same risk-aversion as well

A Conceptual Caveat

- The intertemporal expected utility models presented in this chapter combine risk preferences and time preferences
- Conceptual (often overlooked) caveat within these common models; also may explain some puzzles
- To see this, simply consider expected utility $u(c_1) + \beta E u(C_2)$ where c_1 is certain but C_2 is random
- Then function u captures two aspects of preferences

A Conceptual Caveat (cont'd)

- $u(c_1) + \beta u(c_2)$: the curvature of u captures the desire to smooth consumption across time (elasticity of substitution) under certainty
 - $Eu(C)$: the curvature of u captures risk-aversion, i.e. captures the desire to smooth consumption across states of nature in a static model
- => Not clear why these two different concepts are linked through the **same** utility function $u(\cdot)$

Recursive Preferences

May want to disentangle the two concepts : Kreps and Porteus (1978, Etca), Selden (1978, Etca), Epstein and Zin (1989, Etca)

=> « Recursive preferences »

Built in two different steps:

1) Let $f=v^{-1}(Ev(C_2))$ the certainty equivalent of uncertain period 2 consumption C_2 : atemporal context

2) Let $u(c_1)+\beta u(f)$ the intertemporal preferences w/r to the flow of deterministic consumption: certainty context

Recursive Preferences

In the certainty equivalent, i.e.

$f=v^{-1}(Ev(C_2))$: the function v controls risk-aversion

Within the intertemporal preferences $u(c_1)+\beta u(f)$:
the function u controls the elasticity to substitution

The model thus becomes $u(c_1)+\beta Eu(v^{-1}(Ev(C_2)))$

If $u(.)=v(.) \Rightarrow$ back to the intertemporal expected utility model

Empirical Data

Epstein-Zin (JPE, 1991) examine consumption-portfolio choices under recursive preferences with $v(z) = (z)^{1-\gamma}/(1-\gamma)$ and $u(z) = (z)^{1-\alpha}/(1-\alpha)$

Reject the assumption that $\gamma = \alpha$! (i.e., reject EU)

Elasticity of substitution ($1/\alpha$): α in range [2.4, 4.8]

Relative risk-aversion: γ in range [0.4, 1.4]

Some Other Estimates

| Parameters: | γ | α |
|-------------------------------|----------|----------|
| References: | | |
| Weil (1990) | 45 | 10 |
| Giovanni, Jorion (1991) | #1 | 0.4-1.4 |
| Normandin, St Amour (1996) | 0.4-3.6 | 1.2-3.0 |
| Kocherlakota (1996) | >7 | 0.5-4.5 |
| Chavas and Thomas (1998) | #1 | 0.25 |

5. Physical Risks

Outline:

- State-dependent utility
- A prevention model
- WTP vs. WTA
- Value of statistical life
- Human capital
- Life Insurance

State-Dependent Utility

- Until now, we have assumed that the utility was state-independent: No matter the outcome (or state of the world), same vNM utility $u(\cdot)$
- Sometimes unrealistic to assume state-independence
- The utility function may depend on the « state of the world »

An Example

- Assume two states of the world: either I will be alive (state 1), or dead (state 2)
- The utility should probably be allowed to be different depending on the state of world
- In other words, being dead or alive do not only have financial consequences, but also may directly affect the utility of wealth

More Generally

- State-dependence may be involved for representing preferences w/r to most « physical » risks, e.g. risks to health
- May also include preferences w/r to the environment (pollution, environmental catastrophes, «intangible» damages..)
- Broader class of events: Success vs. failure at love, life with or without kids, loss of freedom, sports' results..

State-Dependent Utility

Foundations:

Fishburn, P., 1970, *Utility Theory for Decision-Making*, Wiley. New York.

Karni, E., 1985, *Decision Making under Uncertainty*, Harvard UP.

Keeney R. and H. Raiffa, 1993, *Decisions with Multiple Objectives*, Cambridge UP.

For what follows, see e.g. Weinstein et al. (1980, JPE) and the book of Jones-Lee (1982), *The Value of Life and Safety*, North-Holland.

State-Dependent Utility

- Axiomatics:

vNM EU can be generalized to state-dependent EU using similar axioms leading to a representation theorem

- No difficulty with objective probabilities

- However identification problem when subjective probabilities are involved: The subjective probabilities cannot be identified from observable choices (see, e.g., Karni, 1985)**

A Prevention Model

- We will first study a particular case of state-dependent model, that is a model of prevention
- There is a possibility of a bad outcome (e.g., death)
- A way to mitigate this risk is to reduce the probability of occurrence of the bad outcome (prevention)

A Prevention Model (cont'd)

There are two states of the world, the good state and the bad state

- $u(w)$ is utility of wealth w in the good state
- $v(w)$ is utility of wealth w in the bad state (e.g., if sick or dead)

Assume $u(w) > v(w)$ and $u'(w) > 0$, $v'(w) \geq 0$ for all w .

A Prevention Model (cont'd)

Let $0 \leq p(e) \leq 1$ the probability that the bad state occurs in which e is the prevention effort (in monetary units)

Assume $p'(e) < 0$ and $p''(e) \geq 0$.

Under (state-dependent) EU, we have:

$$EU = (1 - p(e))u(w - e) + p(e)v(w - e)$$

See, e.g., Weinstein et al. (1980, QJE), Viscusi (1993, JEL)

Optimal Prevention

Maximize $EU = (1-p(e))u(w-e) + p(e)v(w-e)$ over e

FOC:

$$-p'(e)(u(w-e) - v(w-e)) = (1-p(e))u'(w-e) + p(e)v'(w-e)$$

Marginal benefit = Marginal cost

SOC satisfied when $u' > v'$, and u and v weakly concave

What is the Shape of $v(\cdot)$?

Some particular cases:

- $v(w)=u(w-L)$

monetary loss, state-independent

see, e.g., Jullien et al. (2000, GPRIT)

- $v(w)=u(w)-k$

additive separability, strong assumption = same marginal utility of wealth

- $v(w)=ku(w)$ with $0 \leq k < 1$

e.g., if $k=0$, utility if dead with no bequest motive

Viscusi and Evans (1990, AER) estimate $k \approx 0.7$

Prevention and Risk-Aversion

Monetary loss L

Let $EU = (1 - p(e))u(w - e) + p(e)u(w - L - e)$

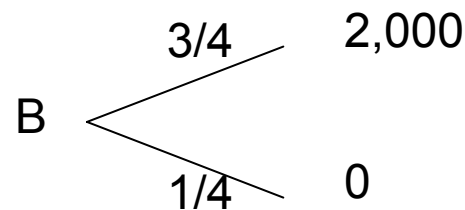
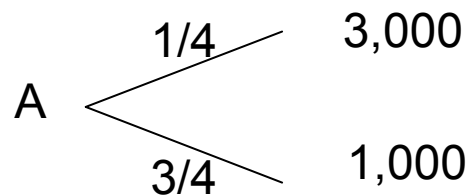
More risk-aversion does not always increase the prevention effort

Dionne and Eeckhoudt (1985, EL)

Intuition?

Prevention and Prudence

- Need condition on u'''
- Eeckhoudt and Gollier (2005, ET) show that a risk averse - and prudent - agent should invest less, and not more, in prevention than a risk-neutral agent!
- Intuition: aversion to a downside risk
- Consider two lotteries:



Same mean and variance

Mortality Risk with No Bequest

Assume $v(w)=0$

$$EU=(1-p(e))u(w-e)$$

Normalize $u(0)=0$

- i) Examine optimal prevention effort under risk-neutrality in wealth (u linear).
- ii) Compare to the effort if risk-averse in wealth (u concave).

Financial risk aversion always increases prevention efforts

Valuation of Mortality Risk Reduction

- Important policy issue
- Suppose one wants to implement a public project that is expected to save lives in the society (e.g., reduce pollution)
- What is the social value of this project?
- How to compare this benefit to the monetary cost of the project?

Valuation of Mortality Risk Reduction (cont'd)

- Benefits from mortality risk reductions often dominate benefit-cost analysis
- E.g., represent a large part of benefits from air pollution reduction programs - see Hammitt (2007) for the US and Pearce et al. (2005) for Europe
- Although the « human capital » approach used to be popular, it is now commonly accepted that benefits from mortality risk reduction should be based on an individual willingness to pay approach

Willingness to Pay

- In our context: maximal amount that an individual is willing to pay for a mortality risk reduction
- Theoretically: The amount that keeps constant the level of expected utility

Russian Roulette

- Pure thought experiment: You have to shoot yourself
- The gun has 10,000 chambers, and 5 of them are loaded with bullets
- You are given the opportunity to remove one bullet before shooting. What is your WTP for this removal?

$$(1-p+e)u(w-WTP) + (p-e)v(w-WTP) = (1-p)u(w) + pv(w)$$

with $p=5/10,000$ et $e=1/10,000$

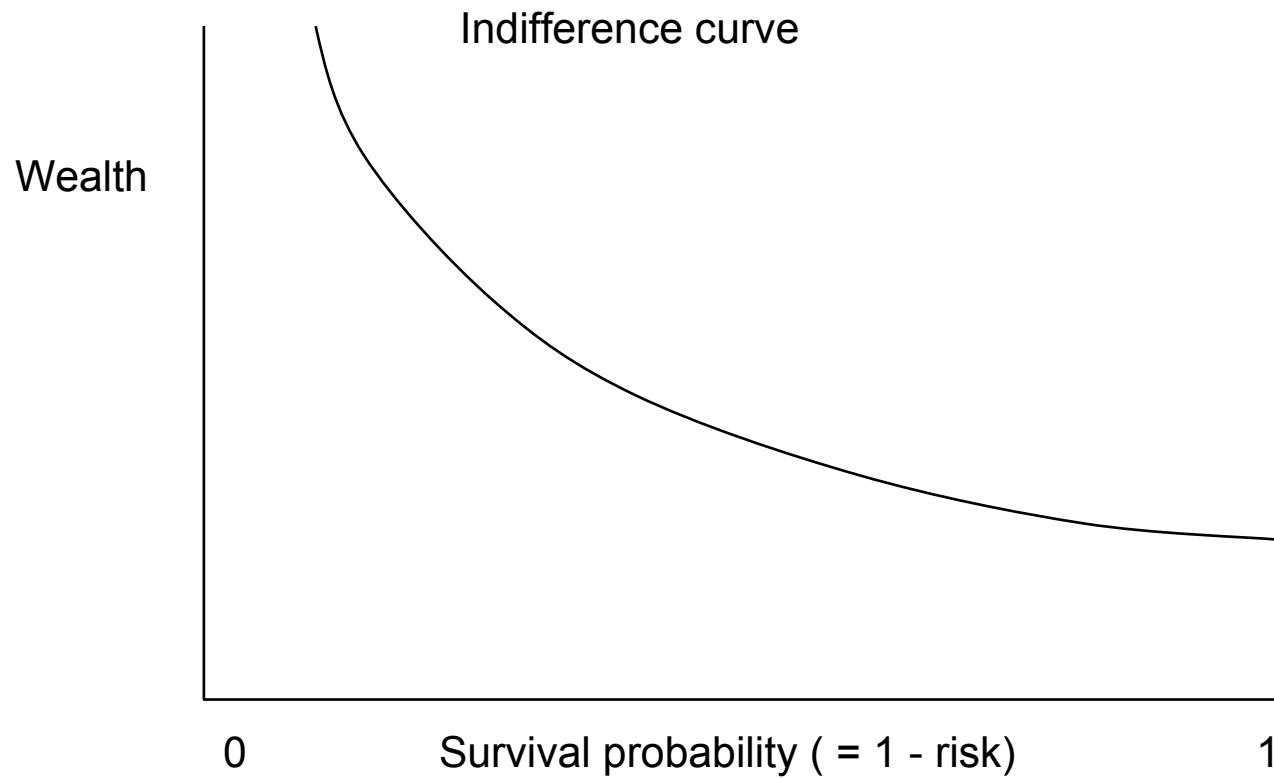
w = initial wealth

$u(.)$ utility if alive; $v(.)$ utility if dead

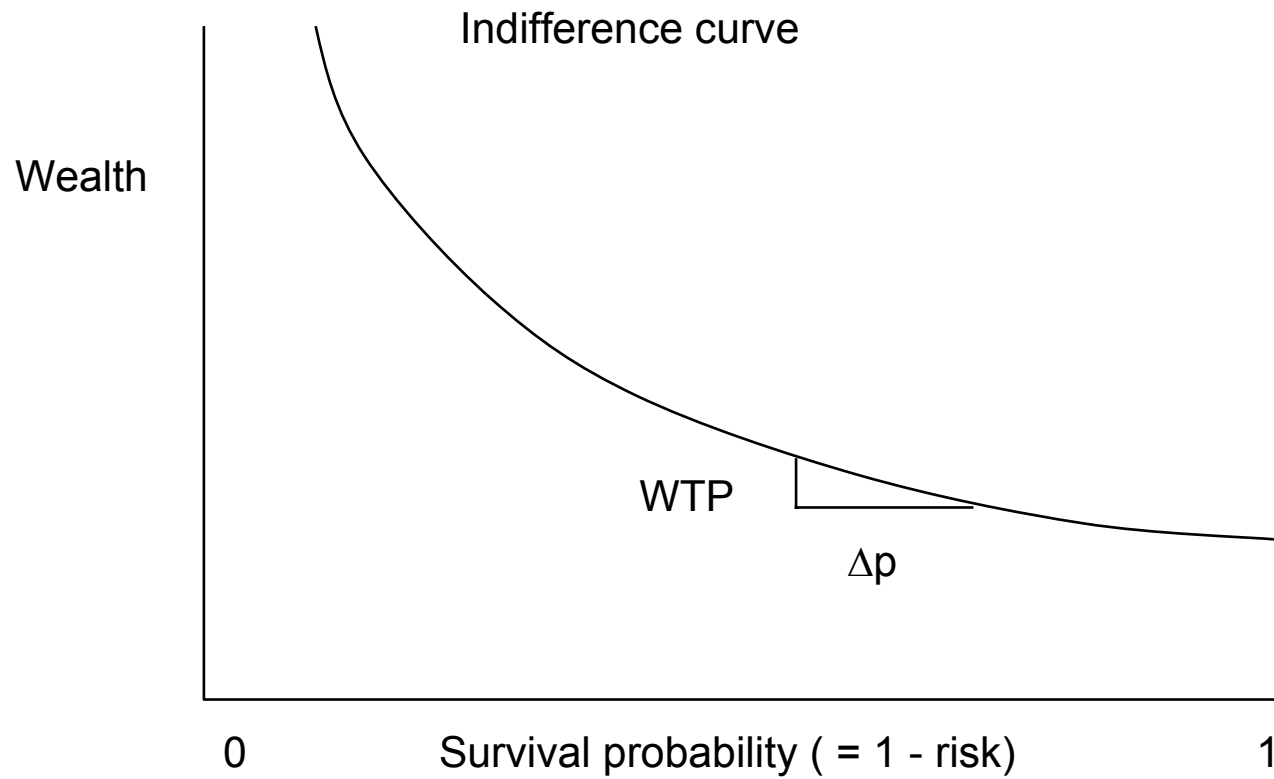
WTP/WTA

- WTA — Willingness to Accept
(Russian Roulette: Which amount would you accept to add one more bullet?)
- WTP is limited by available wealth;
WTA not limited
 - Usually $WTP \leq WTA$
 - For small amounts, $WTP \approx WTA$

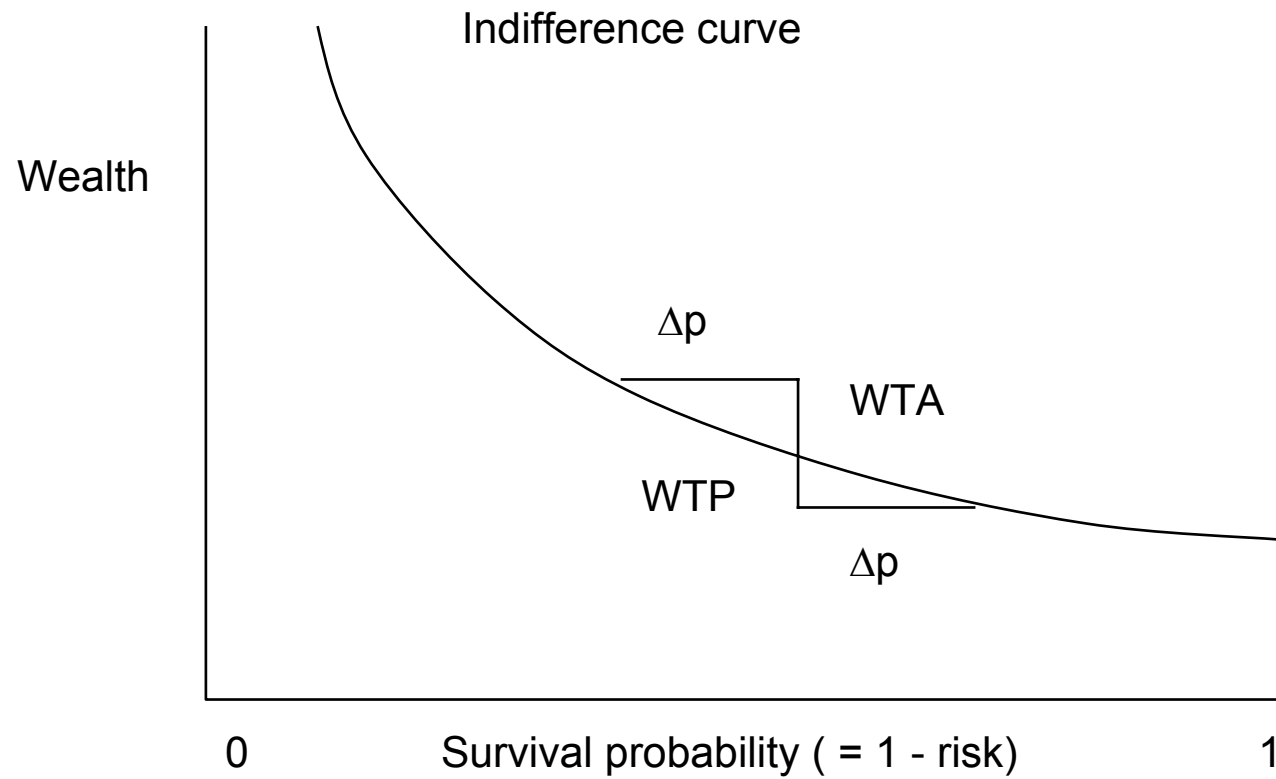
WTP/WTA



WTP/WTA



WTP/WTA



Value of Statistical Life (VSL)

Introduction to the concept:

- N (= 10,000) citizens in a community
- One avoidable statistical death
- WTP equals 500 euros to eliminate this mortality risk of 1/10,000
- VSL is thus 5 million euros total within this community

- $$VSL = \frac{WTP}{\Delta p} = \frac{N \cdot WTP}{N \cdot \Delta p} = \frac{Total_WTP}{E(Life_saved)}$$

VSL : Theory

Let $V=(1-p)u(w) + pv(w)$

VSL: marginal rate of substitution between money and risk

$$VSL = \frac{dw}{dp} = \frac{u(w) - v(w)}{(1-p)u'(w) + pv'(w)}$$

VSL

- Does not measure what an individual is willing to pay to avoid his/her own death with certainty
- It measures WTP (resp. WTA) for an infinitesimal risk reduction (resp. increase)

VSL :

- i) Increases with baseline risk p (“dead-anyway effect”, Pratt and Zeckhauser, 1997, JPE)
- ii) Increases with wealth w (the sum of two effects) under u and v weakly concave

VSL: Calibration

- Let $y=16,500$ euros (french yearly income, INSEE 2004)
- Let $p=3/1,000$ (average yearly death probability for people aged 25-40)
- Let a life expectancy of 45, neglecting changes in income and interest rate, $w=16,500*45=742,500$
- Assume $v=0$, no bequest motive
- Assume constant relative risk aversion equals 0.5

$$VSL = \frac{742,500}{0.997*0.5} \# 1.5 \text{ millions euros}$$

Remark: VSL and Consumption

Let $V = \max_c u(c) + (1-p)\beta u(w - \rho c)$

in which $(1-p)$ is survival probability and c is consumption

VSL: (still) marginal rate of substitution between money and risk

$$VSL = \frac{dw}{-dp} = \frac{u(w - \rho c^*)}{(1-p)u'(w - \rho c^*)}$$

In which c^* is optimal consumption

Estimations of VSL

- \$3 million to \$7 million (US and OECD)
 - \$6.8 million (used by EPA)
 - \$7 million (Viscusi & Aldy, 2003, *JRU*)
- Income-elasticity of VSL positive but usually < 1

| Author | Year | Implicit VSL millions US \$2000 | Country |
|---------------------------|---------|------------------------------------|---------|
| • JOB-MARKET STUDIES | | | |
| • Thaler-Rosen | 1975 | \$1.0 | US |
| • Viscusi | 1978-79 | \$5.3 | US |
| • Dillingham | 1977 | \$3.2-\$6.8 | US |
| • Weiss et al. | 1981 | \$3.9-\$4.5 | Austria |
| • Marin et al. | 1982 | \$4.2 | UK |
| • Moore-Viscusi | 1988 | \$3.2-\$6.8 | US |
| • Berger-Gabriel | 1991 | \$8.6-\$10.9 | US |
| • Cousineau et al. | 1992 | \$2.2-\$6.8 | Canada |
| • Leigh | 1995 | \$8.1-\$16.8 | US |
| • Baranzini et al. | 2001 | \$6.3-\$8.6 | Switz. |
| • Kim | 1993 | \$0.8 | India |
| • Liu et Hammitt | 1997 | \$0.2-\$0.9 | Taiwan |
| • CONSUMER-MARKET STUDIES | | | |
| • Blonquist | 1979 | \$1.0 | US |
| • Atkinson-Alvorsen | 1990 | \$5.3 | US |
| • Dreyfus-Viscusi | 1995 | \$3.8-\$5.4 | US |
| • CONTINGENT VALUATIONS | | | |
| • Johannesson et al. | 1996 | \$5.0 | Sweden |
| • Corso et al. | 2001 | \$3.1 | US 58 |
| • Ludwig-Cook | 2001 | \$6.0 | US |

« Official » VSL for Road Safety

| Countries | VSL Ecus 1994 millions |
|-----------|---------------------------|
| • Germany | 0.79 |
| • Austria | 1.39 |
| • Belgium | 0.37 |
| • Denmark | 0.72 |
| • Finland | 1.21 |
| • France | 0.56 |
| • Grece | 0.13 |
| • Irland | 0.95 |
| • Holland | 0.11 |
| • UK | 1.01 |
| • Sweden | 1.64 |

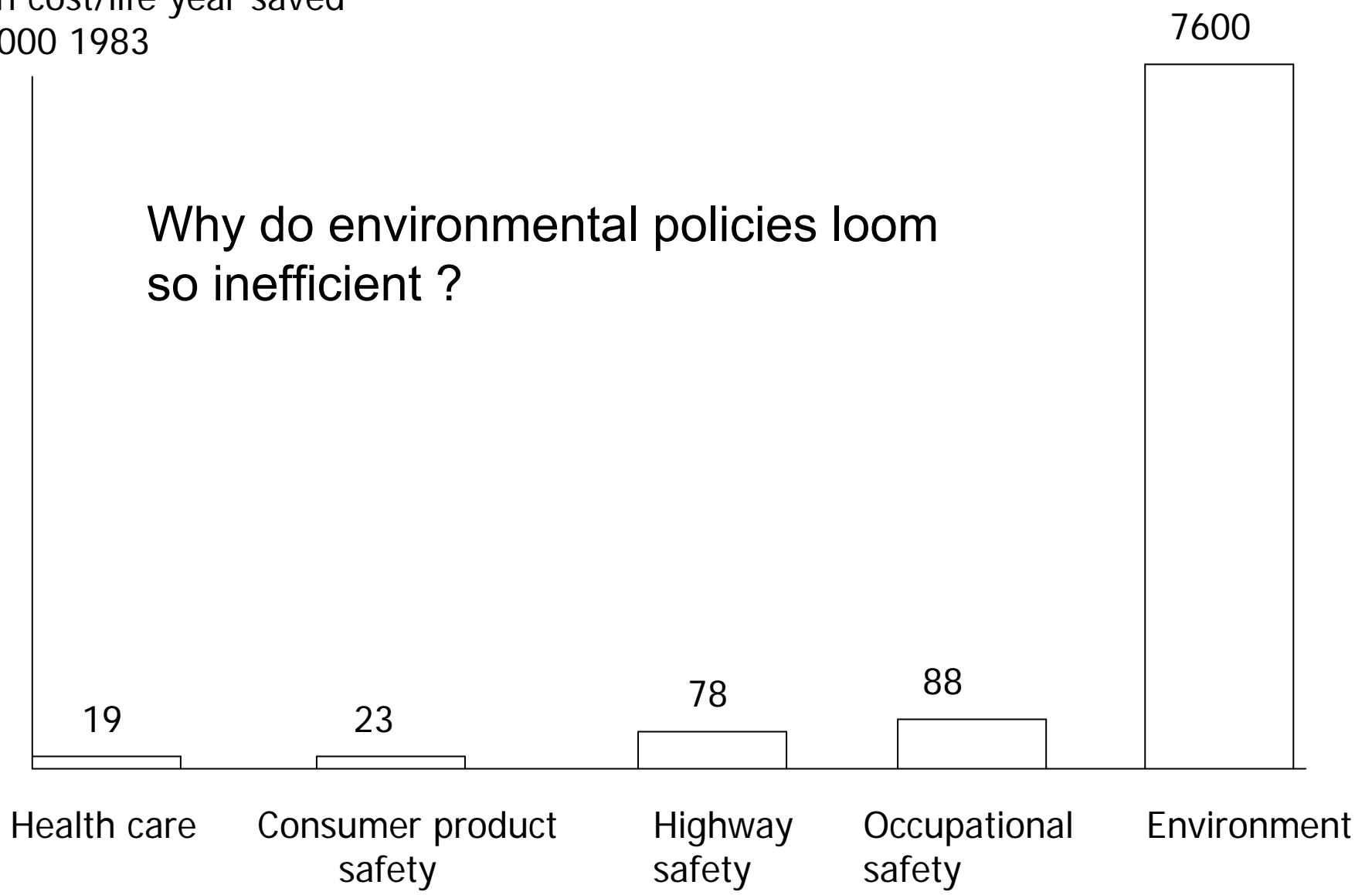
Source: Boiteux (2001)

US Public Prevention Programs

| Programs (Agency) | Estimated cost per avoided death (\$1990) | | |
|--|---|-------------------|---------------------|
| • Underground construction (OSHA) | 0.1 | | |
| • Trihalomethane drinking water standards (EPA) | 0.2 | | |
| • Crane suspended personnel platform (OSHA) | 0.7 | | |
| • Children's sleepwear flammability ban (CPSC) | 0.8 | | |
| • Low altitude windshear equipment (FAA) | 1.3 | Efficient? | |
| • Hazard communication (OSHA) | 1.6 | | |
| • Arsenic/copper smelter (EPA) | 2.7 | | |
| • Grain dust explosion prevention standards (OSHA-S) | 2.8 | | |
| • Radionuclides/uranium mines (EPA) | 3.4 | | |
| • Ethylene dibromide drinking water standard (EPA) | 5.7 | | |
| <hr/> | | | |
| • Abestos occupational exposure limit (OSHA-S) | 8.3 | | Inefficient? |
| • Ethylene oxide (OSHA) | 20.5 | | |
| • Uranium mill tailings (EPA) | 31.7 | | |
| • Abestos ban (EPA) | 110.7 | | |
| • Diethylstilbestrol cattlefeed ban (FDA) | 124.8 | | |
| • Hazardous waste land disposal ban (EPA) | 4,190.4 | | |

Source: Viscusi (1998), Sunstein (2001)

Median cost/life year saved
US \$1000 1983



Why do environmental policies loom so inefficient ?

Source: Tengs and Graham (1996) and Lomborg (2001)

Human Capital

- Traditionally, two conceptual approaches
 - Human Capital
 - VSL
- Human Capital: Opportunity cost of early death, or say earning ability
 - In practice: proportional to net income over lifetime
- What is the link between the two approaches?

Human Capital Table

(\$1,000, in the US, updated from Hartunian et al., 1981)

| Age | Male | Female |
|-------|------|--------|
| 0-14 | 448 | 306 |
| 15-24 | 776 | 525 |
| 25-34 | 868 | 538 |
| 35-44 | 730 | 476 |
| 45-54 | 492 | 370 |
| 55-64 | 199 | 212 |
| 65-74 | 24 | 85 |
| 75 + | 3 | 31 |

WTP vs. Human Capital

- In general, WTP per unit of change in risk is higher than human capital

- Let the WTP to eliminate a mortality risk

$$u(w-WTP) = (1-p) u(w) + p v(w)$$

- Show that if $v(\cdot)=0$ and $u(0)=0$, then $WTP/p > w$ under $u(\cdot)$ concave
- For small p (risk change), $VSL > w$

Implication

- Consider a population of N people, in which Np will die
- Using the WTP approach, we collect ex ante $N \cdot WTP$ to eliminate this mortality risk
- Using the human capital approach, we collect Npw (number of people who die times their human capital w)
- The human capital approach undermines the value of preventing death. It does not take into account preferences (typically financial risk-aversion)

Life Insurance

- Why do people buy life insurance?
- Consider a simple model in which an individual chooses to receive I if he dies:

$$F(I) = (1-p)u(w - (1+\lambda)pl) + pv(w - (1+\lambda)pl + I)$$

where $(1+\lambda)pl$ is the insurance premium

$$\text{FOC: } F'(I) = -(1-p)(1+\lambda)p u'() + p(1 - (1+\lambda)p) v'() = 0$$

SOC satisfied

Life Insurance

$$\text{FOC: } F'(I) = -(1-p)(1+\lambda)u'() + (1-(1+\lambda)p)v'() = 0$$

- Assume that insurance is actuarially fair, $\lambda=0$.

$$\text{FOC: } -u'(w-pl) + v'(w-pl+I) = 0$$

- But by assumption $u'(z) > v'(z)$ for all z , and v' decreasing $\Rightarrow I$ negative is optimal
- “Selling” life insurance is optimal! What’s going on here? Is there something missing?

Life Insurance

Exercise: Find the optimal insurance policy for $u(x)=\text{Log}x$ and $v(x)=k\text{Log}(x)$; assume that the financial loss is Hw if death; and assume $\lambda=0$.

$$I^* = (H+k-1)w / (1+(k-1)p)$$

If $k=1 \Rightarrow I^*=Hw$: full insurance under risk aversion

I^* increases in k , $I^*>0$ when $k>1-H$

I^* (if positive) increases in w (despite DARA!)

Prevention Models: Final Remarks

- Need a general model of prevention with:
 - Individual actions that affect the probability of a loss, but also the loss itself
 - Possibility to purchase life and health insurance contracts
 - Early reference is Ehrlich and Becker (1972, JPE), but few general prevention models exist
- Need a better understanding of the shape of utility in the case of sickness or death

6. Option Values

Outline

- The Concept of Information
- Information Value
- The « Irreversibility Effect »
- The Precautionary Principle

Information

- Information is another, important, way to cope with risk – Allows the decision-maker to better adapt decisions to the knowledge of risk
- Information is obtained from: information search, the passage of time, scientific progress, education, media, social interactions...

Assumption

Information will be

- exogenous (e.g., no learning by doing..)
- non-strategic
- free

Example: Investment Decision

Cost: c , Benefit: X (uncertain). Risk-neutrality.

Investment rule: invest if $EX > c$; Expected profit: **$\max(EX - c, 0)$**

Suppose now perfect information.

Investment rule: invest if $X = x > c$; Expected profit: **$E\max(X - c, 0)$**

Information Value: **$IV = E\max(X - c, 0) - \max(EX - c, 0) \geq 0$**

Take: $c=100$, $X=(50\%, 200, 50\%, 50)$. $IV = 50 - 25 = 25$

Take: $c=100$, $X=(50\%, 140, 50\%, 50)$. $IV = 20 - 0 = 20$

The Concept of Information

- Information, as defined in economics, means that the decision-maker will receive a message about the realisation of X
- The value of information is computed ex ante., i.e. before any message is received. Hence, the decision-maker does not know which message (about the realization of X) will come.

=> The information value is always positive

Positive Information Value

- Let $u(d,X)$ any decision problem in which d is the decision and X a random variable
- Value of information

$$IV = E \max_d u(d,X) - \max_d E u(d,X)$$

Show that IV is always positive

Intuition?

Remark: Information Value

- Value of perfect information: full information versus no information
- Information can be less than perfect
- In economics and statistics: « Better information » is characterized using the Blackwell (1951)'s notion of the comparison of information structures
- Imperfect information not done here.

Determinants of Information Value

- (Small) literature on the determinants of the information value
- The effects of wealth, risk, risk-aversion etc. are all ambiguous. Depends on the decision problem.
- See Hirshleifer and Riley (1992, chapter 5) for a simple and excellent overview

Information and Time

- Information is important in a sequential decision-making framework
- What should I do today given that I will have better information in the future?
- Should I wait? Should I delay decisions? Should I be more cautious?

“Wait and See” Arguments

- DuPont spoken-person (CFC regulation, 1981): *“We are going in a very long way into the regulatory process before scientists know what’s really going on”*
- White House Conference (1990) (CO₂ regulation): *“An aggressive strategy to address possible global change based on today’s knowledge may be wholly inappropriate within a decade”*

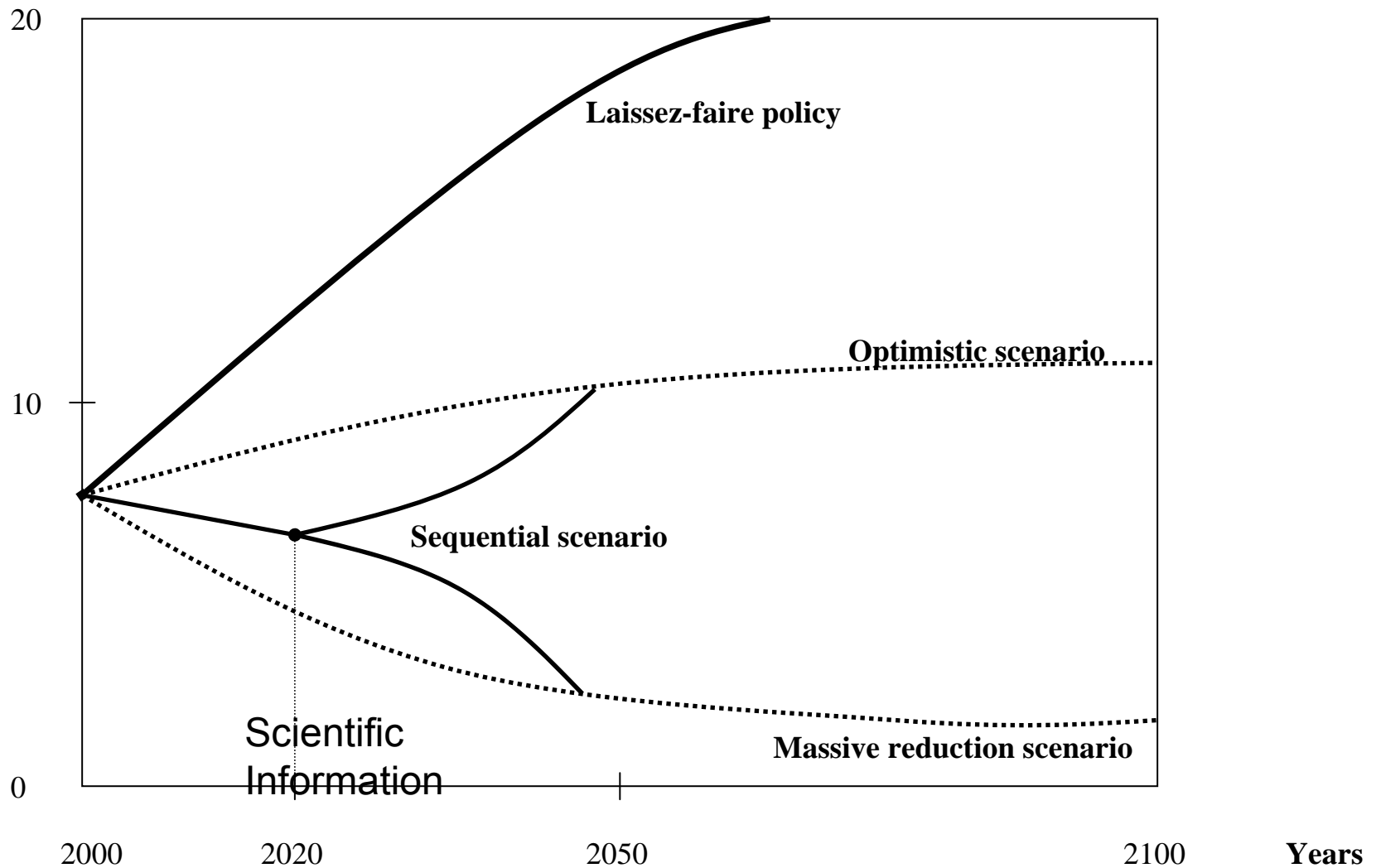
The Precautionary Principle

- Precautionary Principle at Rio Conference (1992) *“Where there are threats of serious or irreversible damage, lack of full scientific certainty shall not be used as a reason for postponing cost-effective measures to prevent environmental degradation”*
- Equivalent Definitions: Loi Barnier (1995), Convention on climate change (1992), Maastricht treaty (1995), Protocol on Biodiversity (2000)...

Over-Cautious?

- Greenpeace: *“Do not admit a substance unless you have proof that it will do no harm the environment”*
- Scientific uncertainty=>refuse any risk-taking
- Inconsistent with economic efficiency and the development of innovations

**Emissions of
CO₂ (GtC/year)**



See: Intergovernmental Panel on Climate Change (IPCC), www.ipcc.ch

Sequential Decision Making

Climate change:

« *The challenge is not to find the best policy today for the next 100 years, but to select a prudent and flexible strategy and to adjust it over time* » (IPCC, 1995)

« *Measures should be periodically reviewed in the light of scientific progress, and amended as necessary* » (European Commission, 2000)

=> Bayesian framework

Prevention vs. Precaution



Reduce the probability
of occurrence of
damages

Static framework

No information arrival



Select flexible and temporary
actions to wait for better
scientific information

Framework : Sequential

Information arrival

See Gollier and Treich (2003, JRU)

Development Project

- A project of development of a forest is considered.
- Total cost c . Current benefit b .
- Future discounted cash-flow X is unknown (e.g., loss of biodiversity)
- Investment Rule: Invest if $b - c + EX > 0$
- Is it the best investment rule?

Alternative Rule

- One may want to wait until we know X .
- An alternative rule may be: « Do nothing today and invest in the future if $X=x>c$ »
- Expected profit of the alternative rule:
 $0+ E\max(X-c,0)$

Alternative Rule

- Reminder: Alternative rule brings $0 + E\max(X-c, 0)$
- To be compared to $\max(b-c+EX, 0)$
- Alternative rule: Loose b but gain the information value
- No info: There is no value of waiting
- With information, the alternative rule may be optimal
- Coined the (quasi-) option Value (Henry, 1974, AER)
- Key features: Information + Irreversibility
- Once the project is developed, cannot be stopped

Modelling the Decision Problem

- Decision Problem- No Information

$$V0 = \text{Max}_{d_1} b d_1 + \text{Max}_{d_2} (EX - c) d_2$$

- Decision Problem- Perfect Information

$$V1 = \text{Max}_{d_1} b d_1 + E \text{Max}_{d_2} (X - c) d_2$$

with d_1 in $D_1 = \{0, 1\}$ and d_2 in $D_2(d_1) = \{d_1, 1\}$

The Decision Problem

Hence we retrieve:

$$V_0 = \text{Max} (b + (EX-c), 0)$$

$$V_1 = \text{Max} (b + (EX-c), E\text{Max}(X-c, 0))$$

Modelling irreversibility constraints:

$D_2(d_1)$ represents irreversibility

If $d_1=0$ then d_2 in $\{0, 1\}$

If $d_1=1$ then $d_2=1 \Rightarrow$ irreversible choice

The « Irreversibility Effect »

- Assume that an *increase* in d_1 shrinks the decision set $D_2(d_1)$ - Does better information leads to *decrease* d_1 ?
- In other words, does it make sense to have more flexibility if better information is forthcoming?

Henry (1974, AER): Yes

Epstein (1980, IER): It depends

The Decision Problem

- Previous payoff (Henry): $v(d_1, d_2, x) = b d_1 + (x - c) b_2$
- General approach (Epstein): unspecified payoff $v(d_1, d_2, x)$
- Epstein (1980) showed that v must have a « separable form » for the irreversibility effect to hold

A Consumption-Resource Model**

- Illustration of non-separable payoff
- A cake can be consumed over three periods. The size of the cake is unknown.
- What is the effect of getting perfect information at date 2 on the consumption at date 1?

Eeckhoudt, Gollier and Treich (2004, EER)

The Consumption Model**

No Info

$$\text{Max } u(c_1) + u(c_2) + E u(X - c_1 - c_2)$$

$$u'(c_2^*) = E u'(X - c_1^* - c_2^*) = u'(c_1^*)$$

Perfect Info

$$\text{Date 2: Max } u(c_2) + u(x - c_1 - c_2) \Rightarrow c_2^{**} = 0.5(x - c_1)$$

$$\text{Date 1: Max } u(c_1) + 2E u(0.5(X - c_1))$$

$$u'(c_1^{**}) = E u'(0.5(X - c_1^{**}))$$

The Consumption Model**

=>under prudence, $c1^{**} > c1^*$: Perfect information increases, and not decreases, consumption!

Intuition:

- Perfect information: perfect smoothing in the future, less risk in the future => less precautionary savings today under prudence
- More information => less « cautious » in the short-run!